



Calhoun: The NPS Institutional Archive
DSpace Repository

Theses and Dissertations

1. Thesis and Dissertation Collection, all items

1969

Verification of model of molten glass flow in a forehearth.

Pekcelen, Sina

Monterey, California. U.S. Naval Postgraduate School

<http://hdl.handle.net/10945/13359>

Downloaded from NPS Archive: Calhoun



Calhoun is the Naval Postgraduate School's public access digital repository for research materials and institutional publications created by the NPS community. Calhoun is named for Professor of Mathematics Guy K. Calhoun, NPS's first appointed -- and published -- scholarly author.

Dudley Knox Library / Naval Postgraduate School
411 Dyer Road / 1 University Circle
Monterey, California USA 93943

<http://www.nps.edu/library>

NPS ARCHIVE
1969
PEKCELEN, S.

VERIFICATION OF MODEL OF MOLTEN
GLASS FLOW IN A FOREHEARTH

by

Sina Pekcelen

United States Naval Postgraduate School



THESIS

VERIFICATION OF MODEL OF MOLTEN GLASS FLOW
IN A FOREHEARTH

by

Sina Pekçelen

December 1969

T131905

*This document has been approved for public re-
lease and sale; its distribution is unlimited.*

Library
U.S. Naval Postgraduate School
Monterey, California 93940

Verification of Model of Molten Glass Flow
in a Forehearth

by

Sina Pekçelen
Lieutenant (junior grade), Turkish Navy
B.S., Naval Postgraduate School, 1969

Submitted in partial fulfillment of the
requirements for the degree of

MASTER OF SCIENCE IN CHEMISTRY

from the

NAVAL POSTGRADUATE SCHOOL
December 1969

1969

PEKCELEN, S

ABSTRACT

In this work, variations on velocity profiles in a flowing mass of molten glass in a forehearth are investigated. Formerly used parabolic velocity profiles are replaced with analytical solution of open channel flow equation, based on the available data on mass flow of molten glass through the channel in unit time.

Concerning the viscosity effects; temperature dependence of viscosity is built in the model. However, it is assumed that the depth of the channel does not affect the viscosity gradients.

To solve the system of non-linear differential equations i.e., heat equation and flow equation; the analytical solution of the latter at the nodes is used for the numeric solution of the former iteratively, until the convergence is obtained. Predicted temperatures are compared to the available data from an actual operating forehearth, and against the results predicted by the previous model using simplifying assumptions to prove its validity.

TABLE OF CONTENTS

I.	INTRODUCTION -----	11
II.	NATURE OF THE PROBLEM -----	12
	A. DERIVATION OF DIFFERENTIAL EQUATIONS -----	16
	B. BOUNDARY CONDITIONS -----	18
	C. NUMERICAL METHOD USED TO SOLVE THE HEAT EQUATION -----	20
III.	VELOCITY PROFILES -----	24
	A. PARABOLIC -----	24
	B. VELOCITY PROFILES USING OPEN CHANNEL FLOW EQUATION -----	24
	C. VELOCITY PROFILES WITH TEMPERATURE DEPENDENCE ----	27
IV.	PHYSICAL PROPERTY PARAMETER ESTIMATION -----	31
V.	DISCUSSION -----	34
	APPENDIX A - GLASS VISCOSITY DATA -----	35
	APPENDIX B - COMPARISON OF RESULTS -----	36
	APPENDIX C - FORTRAN VARIABLES DEFINITIONS -----	38
	APPENDIX D - FLOW GRAPH TO CALCULATE VELOCITIES -----	40
	COMPUTER PROGRAM -----	41
	LIST OF REFERENCES -----	60
	INITIAL DISTRIBUTION LIST -----	61
	FORM DD 1473 -----	63



LIST OF ILLUSTRATIONS

Figure	Page
1. Typical type-K forehearth -----	12
2. Forehearth test section instrumentation end view -----	14
3. Velocity profiles -----	28
4. Viscosity-temperature curve for green glass -----	32

TABLE OF SYMBOLS

A	Radiating area
C	Specific heat
d	Actual channel height
F	Radiating enclosure view factor
h	Channel height - general or convective heat transfer coefficient
k_c	Thermal conductivity - ceramic material
k_{eff}	Effective thermal conductivity
k_{rad}	Radiation thermal conductivity
k_{true}	True thermal conductivity
n	Refractive index
P	Pressure
q	Radiant heat transfer rate
R	Aspect ratio
T	Temperature
T_c	Temperature - ceramic material
T_s	Temperature of radiating surface
V or u	Velocity
\bar{V} or \bar{u}	Average velocity
w	Channel width
W_v	Radiant volume emissive power
γ	Radiant absorption coefficient
ϵ	Value for convergence criteria
ϵ_G	Emissivity of radiating glass surface

ϵ_s	Emissivity of radiating ceramic surface
θ	Time
λ	Radiation wave length
ρ	Density
σ	Boltzmann constant
μ	Viscosity

ACKNOWLEDGEMENT

The author wishes to express his appreciation for guidance and encouragement given him by Professor John Duffin of the Naval Post-graduate School.

I. INTRODUCTION

To improve the production of glass containers, and to transform the art of glass making into a science, the glass industry embarked an extensive forehearth measurement program in an attempt to resolve the complex phenomena of glass conditioning and cooling, while molten glass is taken out of the furnace and transferred to the forming machine.

The objective of the program was the collection of quantitative data to achieve greater understanding of forehearth and to verify the mathematical model of molten glass flow in forehearth developed by Duffin [Ref. 1].

A knowledge of the temperature distribution is needed for better understanding of the control process in glass plants. The above model proved that sophisticated models can give satisfactory results describing the forehearth behavior in a temperature sense. However they need a big computer and require considerable time to run.

In this work, validity of the simplifying assumptions in [Ref. 1] are investigated and ways to relieve them are sought. Going to a more complicated model has academic interest to show that what was developed was a useful and fairly accurate model.

II. NATURE OF THE PROBLEM

Forehearth is that section of the process where molten glass is transferred from furnace to the forming machine. During the flow, glass is conditioned in a temperature sense. A predetermined temperature is desired at the forming machine end, which assures minimum off-grade material after forming process. If undesirable temperature gradients exist at the input of forming machine, recycling of off-grade glassware is necessary, decreasing the overall system efficiency.

What is needed is controlled conditioning throughout the forehearth while molten glass is flowing. This is mainly a heat transfer problem on a flowing mass of molten glass.

To describe the physical phenomenon taking place in a typical forehearth used in glass container manufacture, see Figure (1). Glass flows from left to right in a open channel with dimensions approximately 26 inches wide, 6 inches deep and 18 feet long.

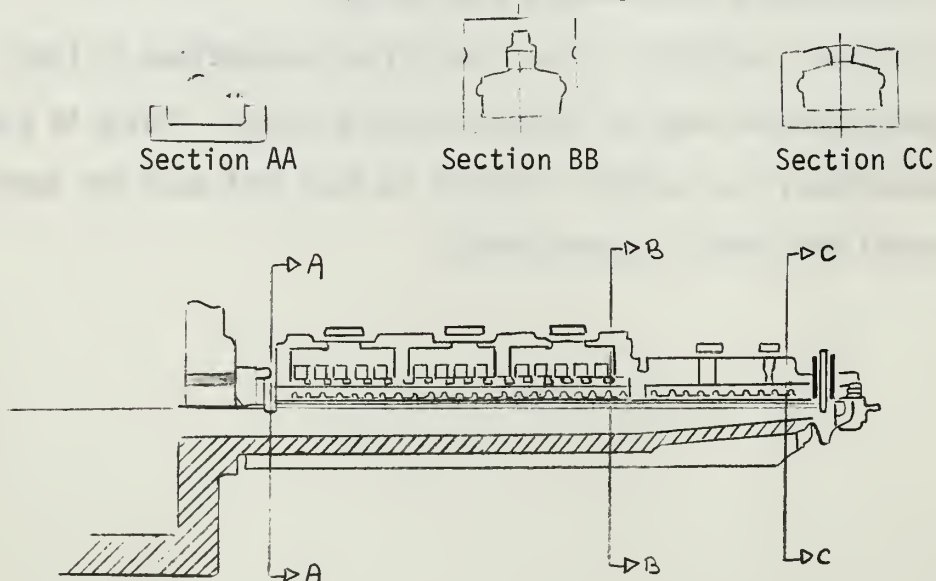


Figure 1. Typical type K forehearth

Section AA is the point of entry from furnace area with average temperature being 2400 degrees F. at this point. Area from AA to BB is called cooling zone. Area from BB to CC is known as conditioning zone. This is the place where an attempt is made to condition the glass so that the delivery temperature would be constant in plane CC. After CC a glass gob is formed. A gob is a discrete mass of molten glass created by intermittently shearing a stream of molten glass coming from an orifice. The gob formed falls into a guide chute, and is conducted to a forming machine mold.

Temperature control is achieved by adjusting burner flame-levels and the amount of cooling wind in the cooling zone (section AA to BB); also with burner flame levels in the conditioning zone.

Burners are mounted on manifolds and are located every 4.5 inches on both sides of the forehearth. They produce a blanket of heat over glass surface. Hot gases sweep over the ceramic radiating surface and heat exchange takes place between gases and surface which, in turn exchanges heat with molten glass. Cooling is achieved by introducing cooling air through inlet pipes. The wind exchanges heat with glass and the ceramic surface and goes out of the system through roof ports. Details of the forehearth cross section is shown in Figure (2).

Heat exchange at the ceramic surface takes place by convection and radiation mechanisms. Heat is also conducted through the ceramic material in the sides and bottom of the forehearth. Possible disturbances can affect the system through these walls.

Above discussion indicates a complex problem of heat exchange in forehearth, with boundaries as described.

To describe temperature behavior within the glass, it is necessary to consider the mechanisms by which heat is transferred.

FOREHEARTH TEST SECTION INSTRUMENTATION END VIEW

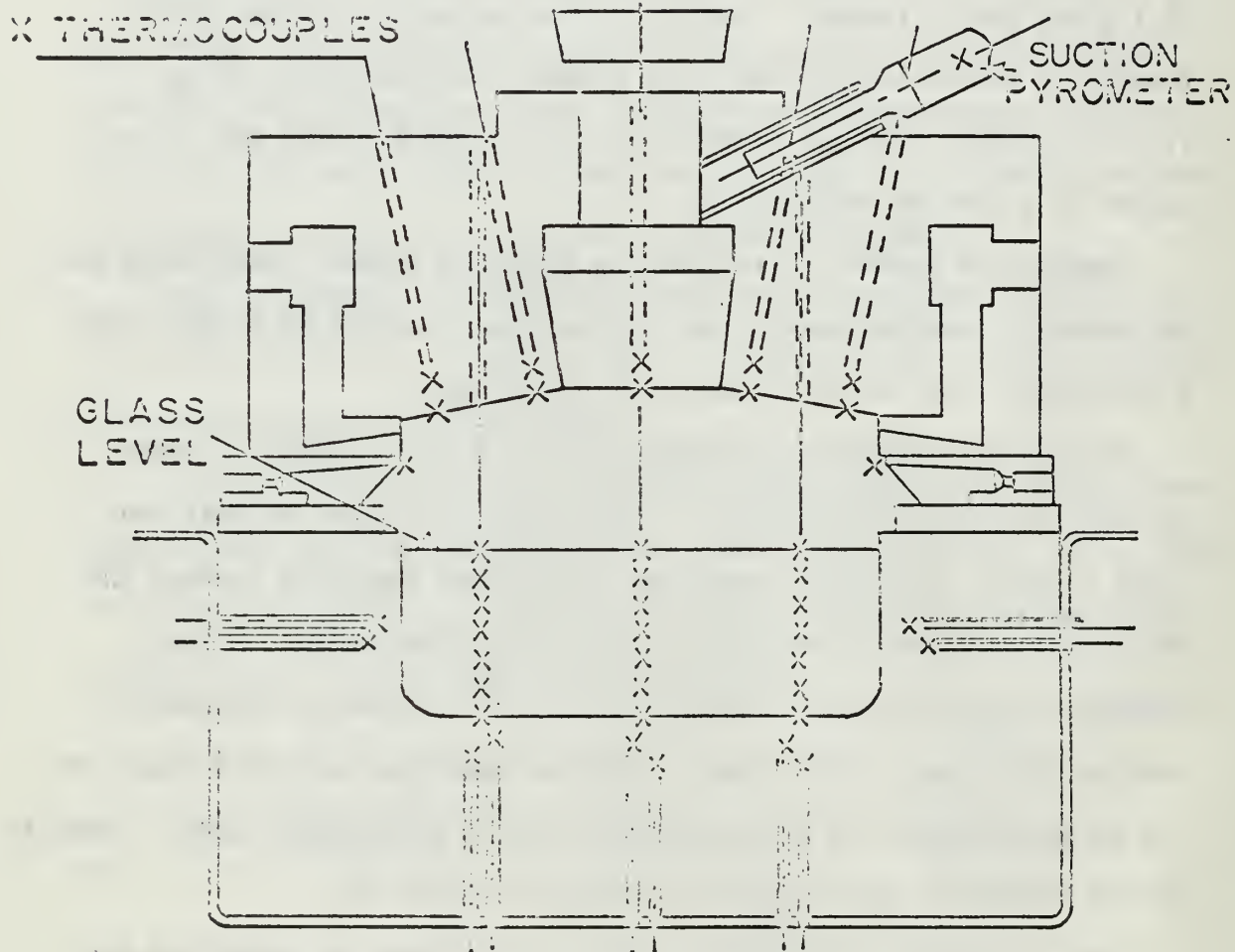


FIGURE 2

It had been shown that emission and absorption of radiation is a bulk phenomena. The interaction of simultaneous emission and absorption throughout the volume leads to radiative heat transfer between adjacent layers of material. When this radiative heat transfer is combined with true conductivity, mathematical description of this internal radiative mechanism becomes rather involved.

Glass is, then, a diathermanous material whose diathermancy is determined by

- a) Wave length-absorption coefficient relation and
- b) Spectral composition of radiation involved.

This dependency is usually shown in plots of absorption coefficient γ versus wave length λ , with temperature as a parameter. Any detailed analysis of the internal radiation should recognize this varying diathermancy. Integration can be replaced by summation using average values of γ for various ranges of λ , with the average value in a given λ range being a function of temperature. Because of its transparency, glass layers beneath the surface will exchange heat with the surroundings. The depth to which this exchange occurs is appreciable varies with the type of the glass being considered. Upper one third of the glass flowing in a forehearth is considered as exchanging energy directly with the surroundings by Duffin [Ref. 1] in his model.

In the glass body, the radiant effects result from bulk phenomena of emission and absorption. Internally emitted radiation is reabsorbed by the glass directly and also as a result of internal reflections. This process leads to the "radiative conductance" of heat through the glass. Internal emission is characterized by "volume emissive power" which is the rate at which a unit volume of glass emits radiation in all directions. For an ideal gray material volume emissive power is given as,

$$W = 4\gamma n^2 \sigma T^4$$

Thus, it is proportional to absorption coefficient, refractive index and Stefan-Boltzman constant. According to Kellet [Ref. 2], in the interior of massive bodies of molten glass, steady-state temperature distributions turn out to be linear. It was also proposed that the effect of radiative conductivity be designated as an "radiation conductivity". For the gray material it is given by

$$k_{RAD} = \frac{16 n^2 \sigma T^3}{3\gamma}$$

Thus, the effective conductivity within the material is the sum of the thermal conductivity and radiation conductivity, as follows:

$$k = k_{eff} = k_{true} + k_{rad}$$

This is set and held throughout the glass depth. But due to dependence on the absorption coefficient, variations are possible near the glass surface.

A. DERIVATION OF DIFFERENTIAL EQUATIONS

Derivation of the differential equations was accomplished by Duffin [Ref. 1] as follows; using a right handed coordinate system and taking X coordinate as the flow direction, a differential volume element of dimensions dx, dy, dz is set up. Then writing energy balance with dz = 1.

1. Energy Into Element Due To Mass Flow

$$\text{Area in X direction} = dy \cdot dz = dy$$

$$\text{Mass flow} = V_x (1 \cdot dy) \rho$$

$$\text{Energy flow} = (\rho dy V_x) (C) (T)$$

2. Energy Out Of Element Due To Mass Flow

$$\frac{\partial}{\partial x} (\rho C V_x T dy) dx + \rho C V_x T dy$$

3. Net Flow Energy

$$= \text{Input} - \text{Output} =$$

$$- \frac{\partial}{\partial x} (\rho C V_x T dx) dy$$

4. Energy Into Element Due To Conduction-Radiation

$$\text{Area} = dx \cdot dz = dx$$

$$\text{Energy} = - k' dx \frac{\partial T}{\partial y}$$

5. Energy Out Of Element Due To Conduction-Radiation

$$\frac{\partial}{\partial y} (- k' dx \frac{\partial T}{\partial y}) dy + [-k' dx \frac{\partial T}{\partial y}]$$

6. Net Conduction-Radiation Energy

$$\frac{\partial}{\partial y} (k' dx \frac{\partial T}{\partial y}) dy$$

7. Net Total Energy Flow

$$\frac{\partial}{\partial y} (k' \frac{\partial T}{\partial y}) - \frac{\partial}{\partial x} (\rho C V_x T) dx dy = (dx dy \cdot \rho) C \cdot \frac{\partial T}{\partial \theta}$$

so, differential equation is

$$\frac{\partial}{\partial y} (k' \frac{\partial T}{\partial y}) - \frac{\partial}{\partial x} (\rho C V_x T) = \rho C \frac{\partial T}{\partial \theta}$$

This being one dimensional model, actual case must include the wall effects which is not considered in above derivation. To account for that, a term for Z direction must be included.

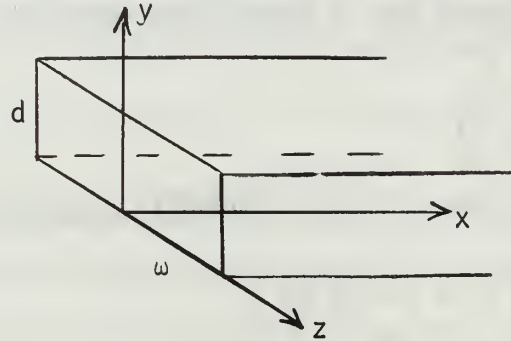
$$\frac{\partial}{\partial y} (k' \frac{\partial T}{\partial y}) + \frac{\partial}{\partial z} (k' \frac{\partial T}{\partial z}) - \frac{\partial}{\partial x} (V_x \rho C T) = \rho C \frac{\partial T}{\partial \theta}$$

If $\frac{\partial T}{\partial \theta}$ is equal to zero, steady-state heat flow equation is obtained.

In above equation density, specific heat and effective conductivity terms can be treated as temperature independent. Dependence of velocity on temperature will be discussed later.

B. BOUNDARY CONDITIONS

To apply boundary conditions, a fixed coordinate system is placed in channel center as follows



$T @ x = 0 \quad y \text{ and } z = 0$ Temperature in the initial plane

$T @ y = d \quad x \text{ and } z = 0$ Radiating boundary

$T @ y = 0 \quad x \text{ and } z = 0$ Bottom temperature distribution

$t @ z = w \quad x \text{ and } y = 0$ Side wall temperature distribution

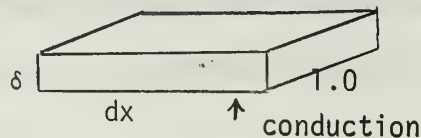
at $y = 0$ and $z = w$ glass contacts with the ceramic material. The temperature of the glass and ceramic material will be same at these points.

Following will also apply

$$\left(\frac{\partial T}{\partial y}\right)_{y=0} = \frac{k_c}{k_r} \left(\frac{\partial T_c}{\partial y}\right)$$

$$\left(\frac{\partial T}{\partial z}\right)_{z=w} = -\frac{k_c}{k_r} \left(\frac{\partial T_c}{\partial z}\right)$$

The boundary at $y = d$ is the radiating boundary. In the model it is assumed that the enclosing surface and the glass surface behave as two infinite opposed parallel planes. If h is the equivalent coefficient of heat transfer for the convection-radiation exchange for the volume element below



Energy Input Area = $dx \cdot l$

$$-k' dx \left(\frac{\partial T}{\partial y} \right)_{y=\delta} + \sigma \epsilon_s T_s^4 dx$$

Energy Output

$$h dx (T - T_s) + \sigma \epsilon_G T^4 dx$$

Accumulation

$$-k' dx \left(\frac{\partial T}{\partial y} \right)_{y=\delta} + \sigma \epsilon_s T_s^4 dx - h dx (T - T_s) - \sigma \epsilon_G T^4 dx = \rho C_p \delta dx \frac{\partial T}{\partial \theta}$$

Let $\delta \rightarrow 0$, so $y \rightarrow d$

$$\left(\frac{\partial T}{\partial y} \right)_{y=d} = \frac{\sigma}{k'} F (T_s^4 - T^4) - \frac{h}{k'} (T - T_s)$$

is the glass to air enclosure boundary condition. F is the view factor which accounts for the geometric arrangement of the two surfaces. With the assumption above following equation applies:

$$F = \frac{1}{1/\epsilon_s + 1/\epsilon_G - 1}$$

Where ϵ_s and ϵ_G are the emissivities of the enclosing surface and glass, respectively. To go one step ahead, this definition of view factor is replaced with a new one, which also accounts for the re-radiation from the connecting walls. Glass and ceramic surface being gray surfaces connected by nonconducting, reradiating walls, the new shape factor is given by Chapman [Ref. 3] as

$$F = \frac{1}{\frac{1}{F_{1-2}} + \frac{A_1}{A_2} \left(\frac{1}{\epsilon_s} - 1 \right) + \left(\frac{1}{\epsilon_G} - 1 \right)}$$

$$F_{1-2} = \frac{A_2 - A_1 F_{1-2}^2}{A_1 + A_2 - 2 A_1 F_{1-2}}$$

F_{1-2} is the geometric shape factor, A_1 and A_2 are the areas of the radiating surfaces.

C. NUMERICAL METHOD USED TO SOLVE THE HEAT EQUATION

Partial differential equation describing the steady-state temperature $T(x,y,z)$ in a moving rectangular slab of molten glass in a forehearth is

$$\frac{k'}{\rho C_p} \frac{\partial^2 T}{\partial y^2} + \frac{k''}{\rho C_p} \frac{\partial^2 T}{\partial z^2} - \frac{\partial}{\partial x} (V_x T) = 0 \quad (2.1)$$

Where cartesian coordinates are used, x is the flow direction down the length of the slab from the front of the hearth, y is the direction from the bottom channel toward the top of the slab, and z is the direction from the channel center toward the side. k' , k'' , C_p are the known constants. The initial temperature distribution at $x = 0$ is assumed to be linear in y and z . It can be found by linear interpolation from the four corner temperatures. Similarly it is assumed that the temperature on the boundaries ($y = 0$), bottom of the channel, and ($z = w$), side of the channel, are also linear. I.e.,

$$T(0,y,z) = \phi_1(y,z) \quad (2.2)$$

$$T(x,0,z) = \phi_2(x,z) \quad (2.3)$$

$$T(x,y,w) = \phi_3(x,y) \quad (2.4)$$

and are all known. The temperature of the glass is symmetric with respect to the center line ($z = 0$); therefore,

$$\left(\frac{\partial T}{\partial z}\right)_{z=0} = 0 \quad (2.5)$$

Radiative boundary at the surface of the glass ($y = d$) is that of radiative and convective heat transfer. Equation derived previously was,

$$\left(\frac{\partial T}{\partial y}\right)_{y=d} = \frac{\sigma}{k} F(T_s^4 - T^4) - \frac{h}{k} (T - T_a)$$

Using linearizing approximation on the nonlinear part, and changing sign on the second term of right hand side,

$$\left(\frac{\partial T}{\partial y}\right)_{y=d} = \frac{4\sigma F}{k'} (T_s + 460)^3 (T_s - T_{y=d}) + \frac{h}{k'} (T_a - T_{y=d}) \quad (2.6)$$

Where σ , F , k' , h are known constants. T_a is the air temperature on the glass surface. T_s , the temperature of surroundings is determined by linear interpolation between the temperature at the center of the channel, T_{s0} and the known temperature on the boundary at the side ($z = w$). The center temperature is assumed to decrease linearly from initial temperature T_{s1} at $x = 0$ by an amount T_c , at the end of the channel ($x = XL$); therefore

$$T_{s0} = T_{s1} - \frac{X}{XL} T_c$$

With these, the problem is formulated as being the solution of the partial differential equation (1), with initial condition (2.2), and boundary conditions (2.3), (2.4), (2.5), and (2.6).

An unconditionally-stable alternating-direction method [Ref. 4] was applied after passing equation (1) into finite difference form. This is accomplished by first getting the first derivatives with backward differences then substituting these in forward difference equation to get finite difference equation for second space derivatives, in y and z directions. Forward difference form is used for the derivative in x direction.

The first increment step is taken as implicit in y direction, the second implicit in z direction, and so on, x step size being the same in each case. Temperatures at successive planes in x direction are related to each other since the first step involves values at $x + \Delta x$ and these intermediate values $(T_{i,j}^{*n+1})$ are used in the following step during the numeric calculation. System of equations obtained are,

$$b_{ij}(T_{i,j}^{*n+1} - T_{i,j}^n) = C_1(T_{i-1,j}^{*n+1} - 2T_{i,j}^{*n+1} + T_{i+1,j}^{*n+1}) + C_2(T_{i,j-1}^n - 2T_{i,j}^n + T_{i,j+1}^n)$$

$$b_{ij}(T_{i,j}^{n+1} - T_{i,j}^{*n+1}) = C_1(T_{i-1,j}^{*n+1} - 2T_{i,j}^{*n+1} + T_{i+1,j}^{*n+1}) + C_2(T_{i,j-1}^{n+1} - 2T_{i,j}^{n+1} + T_{i,j+1}^{n+1})$$

With following definitions using increments Δx , Δy , Δz

$$b_{ij} = V_x(i\Delta x, j\Delta z)$$

$$C_1 = \frac{1/2\Delta x}{\Delta y^2} \frac{k'}{\rho C_p}$$

$$C_2 = \frac{1/2\Delta x}{\Delta z^2} \frac{k''}{\rho C_p}$$

$$T_{i,j}^n = T(n\Delta x, i\Delta y, j\Delta z)$$

$$T_{i,j}^* = T(n\Delta x, i\Delta y, j\Delta z)$$

The indice i runs from $i = 1$ to $i = I$ where $i \cdot \Delta y = d$, indice j runs from $j = 0$ to $j = J-1$ where $j \cdot \Delta z = w$. The initial temperature gives the values $T_{i,j}^0 = \phi_1(y, z)$, boundaries give the values $T_{0,j}^n = T_{0,j}^{*n} = \phi_2(n\Delta x, j\Delta z)$ when $i = I$ and $T_{i,J}^n = T_{i,J}^{*n} = \phi_2(n\Delta x, i\Delta y)$ when $J = J-1$.

Also, symmetry around the center line of the channel gives rise to $T_{i,-1}^n = T_{i,1}^n$ and $T_{i,-1}^* = T_{i,1}^*$ when $j = 0$. Radiating boundary results in substitutions for $T_{i+1,j}^n$ and $T_{i+1,j}^{*n}$ in terms of $T_{i,j}^n$ and $T_{i,j}^{*n}$ when $i = I$. ϕ_1 , ϕ_2 and ϕ_3 are obtained from corner temperatures by linear interpolation.

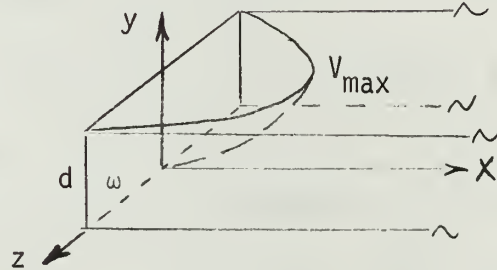
The system of equations is solved starting from $T_{i,j}^0$, getting the intermediate solution from the first and using it in the second, making use of Thomas algorithm [Ref. 5] to solve resulting tridiagonal matrices, and proceeding through the channel at every y, z plane separated by

Δx in x direction, until the end of the test section is reached ($x = XL$). For integration purposes x length of the channel is divided into 500 increments ($\Delta x = XL/500$), y coordinate is divided into 30 increments, and z coordinate is divided into 75 increments, making use of the symmetry around the center line.

III. VELOCITY PROFILES

A. PARABOLIC

First considerations of velocity distribution within the flowing mass of molten glass by Duffin [Ref. 1] had involved moving side walls of the channel to infinity which gave velocity in x direction as a simple function of y coordinate. Next step was evaluation of finite velocity step surfaces based on a given mass flow rate of glass in an effort to account for higher velocities in the center channel and lower velocities near the side walls and bottom. None proved satisfactory, so final choice was the use of explicit expressions for parabolic velocity profiles. Physical picture is as follows:



Maximum velocity occurs at $y = d$ and on center line $z = 0$. Derivation of the general equation of parabola families gives velocity in x direction as a function of y and z, and physical parameters w, d and V_{\max} as follows:

$$V_x(y,z) = V_{\max} \left[1 - \left(\frac{y}{d}\right)^2 - \left(\frac{z}{w}\right)^2 + \left(\frac{yz}{dw}\right)^2 \right] \quad (3.1)$$

from which $9/4 V_{\text{ave.}} = V_{\max}$ can be obtained. After integration over the channel cross section and dividing by channel area.

B. VELOCITY PROFILES USING OPEN CHANNEL FLOW EQUATION

Above parabolic profile does not account for the viscosity-temperature relationship. Cooper [Ref. 6] pointed out that the effects of moderate

viscosity gradients on velocity are negligible. Temperature in the forehearth changes from 2400°F to 2000°F and across this temperature range viscosity varies by a factor of ten. It has been shown that a viscosity change of 5×10^5 would affect velocity only by factor of three. These facts justify the assumption of constant velocity profiles through the channel length.

To investigate the possible outcome when above assumption is relaxed, parabolic profiles are replaced with the solutions of the differential equation describing laminar flow in open channels. The differential equation to be solved is

$$\frac{\partial}{\partial y} \left(\mu \frac{\partial u}{\partial y} \right) + \frac{\partial}{\partial z} \left(\mu \frac{\partial u}{\partial z} \right) - \frac{dp}{dx} = 0. \quad (3.2)$$

Where x is the direction of the flow, u is the velocity, and μ is the viscosity. Channel width is taken as w and depth being h . A coordinate system is set at the midstream center with boundary conditions:

$$u = 0 \quad @ \quad z = w \quad (3.3)$$

$$u = 0 \quad @ \quad y = h$$

$$\frac{du}{dy} = 0 \quad @ \quad z = 0$$

$$\frac{du}{dz} = 0 \quad @ \quad z = 0$$

If viscosity can be considered to be independent of depth and width, above equation simplifies into

$$\frac{\partial^2 u}{\partial y^2} + \frac{\partial^2 u}{\partial z^2} - \frac{1}{\mu} \frac{dp}{dx} = 0 \quad (3.4)$$

which is solved with its boundary conditions by the use of infinite series.

Solution taken from Timoshenko and Goodier [Ref. 7] is

$$u = \frac{16\lambda h^2}{\pi^3} \sum_{n=1,3,5,\dots}^{\infty} \frac{1}{n^3} (-1)^{\frac{n-1}{2}} \left[1 - \frac{\cosh \frac{n\pi z}{2h}}{\cosh \frac{n\pi w}{2h}} \right] \cos \frac{n\pi y}{2h} \quad (3.5)$$

Integrating over the area of half-section and dividing by the area ($h \cdot w$) gives the mean velocity \bar{u} .

$$\bar{u} = \frac{32\lambda h^2}{\pi^4 w} \sum_{n=1,3,5,\dots}^{\infty} \frac{1}{n^4} \left(w - \frac{2h}{n} \tanh \frac{n\pi w}{2h} \right) \quad (3.6)$$

Data for the average mass flow rate gives an estimate for \bar{u} value, which in turn can be used to get a value for λ . An experimental value of \bar{u} from GCIRC report [Ref. 8] was 7.77 ft/hour for green glass. This is used in a computer program to evaluate λ taking ten terms of the series (3.6). Result was 0.03649. With that value, velocity at every node of the initial plane is calculated and held constant through the channel, as a first try to change previously used profiles. To give an idea about the difference obtained in velocity profiles, isovels are plotted by 3.0 ft/hour increments in Figure (3b). These changes of main computer program increased the running time considerably. Steady-state results are reported in Appendix (B), under run (A) for $\bar{u} = 7.77$, run (B) for $\bar{u} = 8.54$ and run (C) for $\bar{u} = 7.00$. Purpose of the last two runs was to get an idea about the effect of mass flow rate on the temperature distribution, since the reported value is just a close estimate of the actual mass flow rate in the forehearth. Generally better correlation is observed to actual data in the center line temperatures, but rather poor results observed toward the walls of the channel. Maximum deviation of 15 degrees F. is calculated in these three runs.

C. VELOCITY PROFILES WITH TEMPERATURE DEPENDENCE

To build in the viscosity-temperature dependence, available viscosity data, Appendix (A), is fitted to a functional form as,

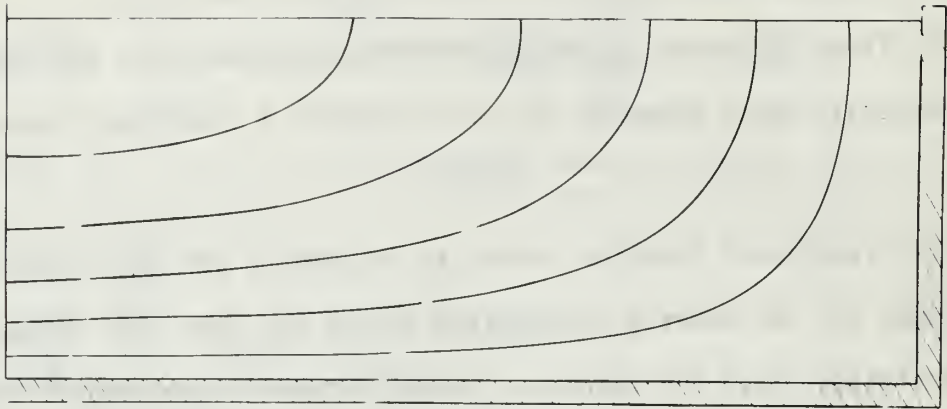
$$\mu = e^{a+bT}$$

This functional form for viscosity is used to get the values of μ at the nodes for the numeric calculation and at the same time employing an estimated value for (dp/dx) . Isovels depending on initial temperature distribution are shown in Figure (3c).

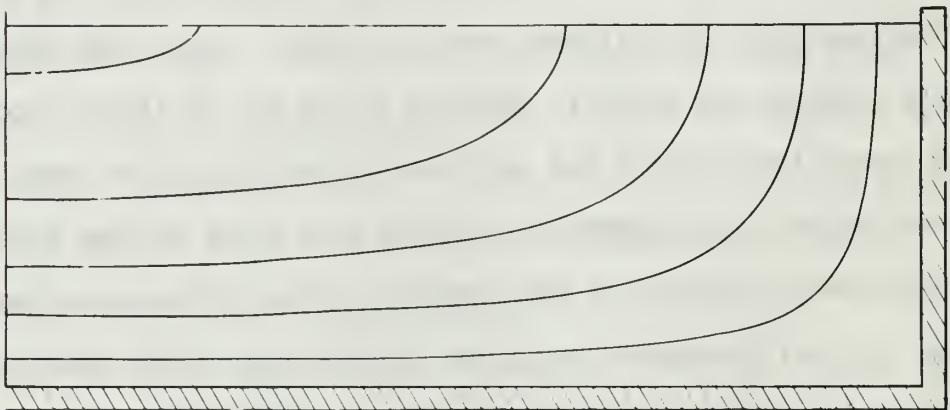
To solve the partial differential equations i.e., heat equation and flow equation, the following route is taken: Start with initial temperature distribution which is obtained by the use of linear interpolation of corner temperatures and calculate velocities at the nodes. Based on these velocities, temperatures in the next plane in flow direction are calculated by the use of the computer program already developed. All the physical parameters are taken as they were in the previous parabolic constant velocity profile computations. Computed temperatures at the nodes are used to recompute the velocity distribution, which is compared with the first velocity array until they agree within the small value ϵ . Iterative technique is used in the following way: the first velocity array is stored in BA (i,j) array for comparison purposes; after the computation of temperatures in one step down the flow direction, they are used to get the new velocity array BIJ (i,j). If those two do not agree when compared at every node of the plane, a linear combination of the two arrays is taken as

$$BIJ(i,j) = W_a \cdot BA(i,j) + (1 - W_a)BIJ(i,j)$$

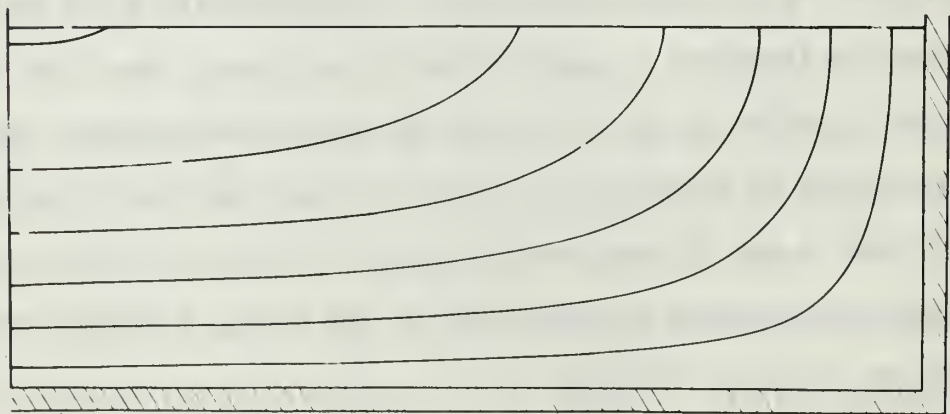
where W_a is a weight factor. The BIJ(i,j) array is stored in BA(i,j)



A. Isovels using Parabolic Equation.



B. Isovels using Open Channel Flow Equation.



C. Isovels with Temperature Dependence

Figure 3. Isovels for Channel Flow

as the new velocity array, and above cycle is repeated until convergence is obtained. Flow diagram is shown in Appendix (D). Numerous runs for the first two planes proved that the above method is appropriate. Value of W_a is varied to have an idea of its influence on the convergence and also on time to run. Final decision was $W_a = 0.25$ since it cuts the running time by half when compared to $W_a = 0.75$.

Due to the inevitable increase in the computer time with the above scheme, instead of updating the velocity array at every Δx increment this is done at every 50 Δx increments. This is updating the velocity array ten times through the channel length. By the trial runs to assign a value to ϵ , it is found that it takes more than 18 iterations for the convergence with $\epsilon = 0.001$. Five iterations are needed when $\epsilon = 0.01$ and 216 seconds to calculate the temperatures at $x = \Delta x$ and $x = 2 \Delta x$. Taking these facts into consideration and also considering the reliability of the data, choice of $\epsilon = 0.1$ is considered appropriate. For run (D) velocity array is corrected with 50 Δx increments, ϵ value was 0.1, running time 1/4 hour. Results at the nodes where data was taken was comparable to the best run obtained with the constant velocity calculations but not any better. In subsequent runs (D) and (E) the estimate of (dp/dx) is increased by 10% and 15% respectively, giving closer fit to the actual data. The absolute average deviation was around 4.6 degrees F. in all above runs. The largest deviation observed was at $y = 5.88$ inches and $z = 8.63$ inches with values around -15 degrees F. This deviation was also present in the results of the previous model. Another variation tried to compute velocity array using 25 Δx increments. Results are reported under run (F). No improvement is observed but running time is increased to twenty minutes.

In run (G), boundary temperature at $x = XL$, $y = d$ and $z = w$ was decreased from 2078°F to 2035°F , and velocity updated with $50 \Delta x$ increments. Thus run gave the smallest absolute average deviation 4.2°F between data point temperatures and predicted temperatures. All above runs compute velocity array at the nodes using 10 terms of the defining series equation (3.5). When 5 terms of the series is employed running time decreased more than three minutes. The last run in these lines was run (H) with 5 terms for velocity calculation, ϵ value of 0.1, and radiating boundary temperature at the channel corner is increased to 2140°F from originally used 2125°F . It took 11.8 minutes to run, maximum deviation was 12.1°F being 1.8°F less than the best result obtained with the previous model. Absolute average deviation from data was 4.22°F . In run (I), previously used view factor is replaced with the new one, accounting for the reradiation from the channel walls. Maximum deviation from the data was 10.6°F , and absolute average deviation was 4.7°F . The predicted temperatures at data points for all above runs are listed in Appendix (B).

VI. PHYSICAL PROPERTY-PARAMETER ESTIMATION

Physical properties used in the equations must be estimated or calculated. Many of these properties and parameters are set at values used in the previous model. Since this work is based on the green glass only, important parameters that were used in original model for that kind of glass are listed below.

Radiation Conductivity	k'	10.0	BTU/HR.FT. F
Density	ρ	147.77	LBS/FT.
Specific Heat	C_p	0.375	BTU/LB. F
Radiant Surface Emissivity	ϵ_s	0.9	
Glass Surface Emissivity	ϵ_G	0.9	
Convective Heat Coefficient	h	20.0	BTU/HR.FT. F

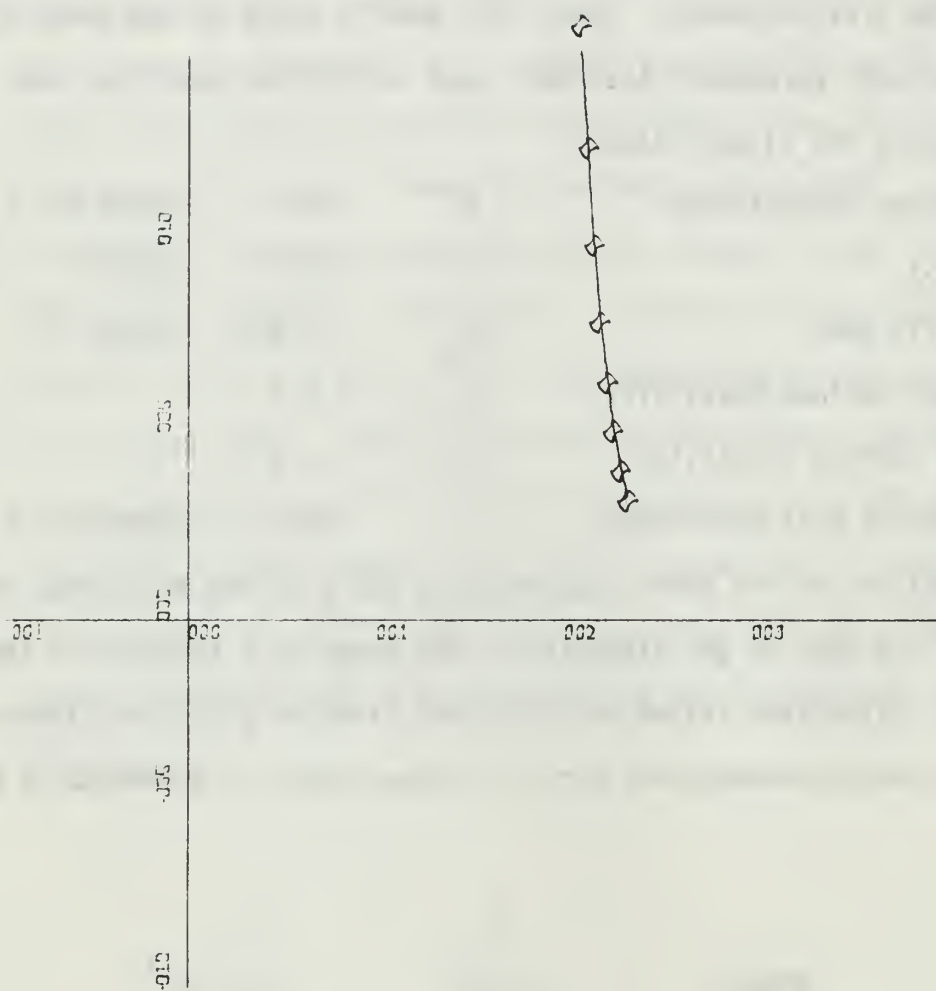
In addition to the above, parameters a and b in the functional form $\mu = e^{a+bT}$ are used to get viscosity at the nodes as a function of temperature. Calculated values for different kinds of glass are given below. Plotted viscosity-temperature curve for green glass is presented in Figure (4).

	<u>a</u>	<u>b</u>
Green	9.07	$2.82 \cdot 10^{-3}$
Flint	8.60	$2.60 \cdot 10^{-3}$

To estimate (dp/dx) value; first λ is calculated from the average velocity data based on the mass flow rate, then this value is used together with the average viscosity, since λ is defined as

$$\lambda = \frac{1}{\mu} (dp/dx)$$

Calculated value for (dp/dx) is $6.849 \cdot 10^{-4}$.



* SCALF -1.00E+03 UNITS INCH.
 * SCALF -5.00E+02 UNITS INCH.
 PEKCELEN WG27
 GREEN GLASS

Figure 4. Viscosity-Temp Curve.

In view factor calculations, which account for the reradiation from the channel walls, areas of the radiating surfaces are assumed to be equal. Emissivity values are not changed. Geometric view factor is taken from Chapman [Ref. 3] as 0.56.

V. DISCUSSION

Comparison of the results obtained by the previous and modified models made it clear that the assumption of constant velocity distribution through the channel does not have significant effect on the final results. Predicted temperatures at the nodes were still off by small values. Model generally proved flexible and stable for all variations made of velocities and of boundary conditions. It still does not account for the possible viscosity changes due to pressure changes, since pressure changes with position. However, this is not considered significant since putting in viscosity-temperature dependence proved that initial velocities at the nodes decrease by 20-60% depending on the position. Further work could involve putting in functional forms for density, heat-capacity and thermal-conductivity to build in the temperature dependence of these parameters. If this is done, the model will be further complicated and limit its possible use in a closed loop computer control system. To serve for control purposes, time consumption should be decreased considerably. This will be possible only by the use of some simplifications. If the accuracy in positioning of thermocouples and reliability of the temperature data is considered, the present form of the model gives rather good agreement for the steady-state temperature data. It can possibly be used for design purposes. Requirement for a powerful computer is also a drawback for control purposes. An alternate route might be use of a hybrid computer instead of a digital one to make use of the fast integration abilities of analog computers to decrease the running time.

APPENDIX (A)

GREEN GLASS VISCOSITY DATA

<u>Temperature°F</u>	<u>Viscosity (Centipoises)</u>
2330.4	316.2
2292.9	398.1
2255.5	501.2
2221.1	631.0
2185.7	794.3
2153.1	1000.0
2121.2	1259.0
2089.4	1585.0

APPENDIX (B)

Comparison of data and results predicted with models for green glass

Thermocouple position (in.)
relative to (0,0,0) point

<u>X</u>	<u>Y</u>	<u>Z</u>	<u>Data</u>	Previous		<u>Run(A)</u>	<u>Δ</u>	<u>Run(B)</u>	<u>Δ</u>	<u>Run(C)</u>	<u>Δ</u>	<u>Run(D)</u>	<u>Δ</u>
				<u>Model</u>	<u>Δ</u>								
37.5	5.88	0.0	2127.0	2127.5	+0.5	2123.8	-3.8	2125.9	-1.1	2122.2	-4.8	2123.7	-3.3
			2095.0	2081.1	-13.9	2083.9	-11.1	2086.6	-8.4	2082.1	-12.9	2079.8	-15.2
37.88	4.88	0.0	2145.0	2146.0	+1.0	2141.7	-3.3	2144.4	-0.6	2138.3	-6.7	2142.5	-2.5
			2100.0	2096.0	-4.0	2100.7	+0.7	2104.6	+4.6	2097.4	-2.6	2094.8	-5.2
38.25	3.88	0.0	2147.0	2153.0	+6.3	2148.9	+1.9	2152.3	+5.3	2145.0	-2.0	2150.8	+3.8
			2095.0	2101.0	+6.0	2106.2	+11.2	2110.7	+15.7	2102.1	+7.1	2099.9	+4.9
39.00	1.88	0.0	2145.0	2142.1	-2.9	2139.2	-5.8	2141.6	-3.4	2136.2	-8.8	2140.5	-4.5
			2077.0	2085.6	+8.6	2088.5	+11.5	2090.0	+13.0	2085.1	+8.1	2082.8	+5.8
39.38	0.88	0.0	2132.0	2129.8	-2.2	2127.8	-4.2	2129.1	-2.9	2126.3	-5.7	2128.1	-3.9
			2062.0	2069.2	+7.2	2068.4	+6.4	2070.0	+8.0	2066.6	+4.6	2064.9	+2.9
39.75	0.0	0.0	2122.0	2122.0	0.0	2122.0	0.0	2122	0.0	2122.0	0.0	2121.9	-0.1
			2052.0	2051.7	-0.3	2054.8	+2.8	2047.3	-4.7	2047.3	-4.7	2048.4	-3.6

Thermocouple Position (in.)
relative to (0,0,0) point

<u>X</u>	<u>Y</u>	<u>Z</u>	<u>Data</u>	<u>Run(E)</u>	<u>Δ</u>	<u>Run(F)</u>	<u>Δ</u>	<u>Run(G)</u>	<u>Δ</u>	<u>Run(H)</u>	<u>Δ</u>	<u>Run(I)</u>	<u>Δ</u>
37.50	5.88	0.0	2127.0	2124.9	-2.1	2120.4	-6.6	2126.9	-0.1	2125.3	-1.7	2130.1	+3.1
		8.63	2095.0	2081.0	-14.0	2076.5	-18.5	2079.2	-15.8	2082.9	-12.1	2086.8	-8.2
37.88	4.88	0.0	2145.0	2144.4	-0.6	2138.3	-6.7	2144.5	-0.5	2144.6	-0.4	2148.2	+3.2
		8.63	2100.0	2097.2	-2.8	2090.2	-9.8	2094.0	-6.0	2098.9	-1.1	2101.7	+1.7
38.25	3.88	0.0	2147.0	2152.8	+5.8	2146.2	-0.8	2152.8	+5.8	2153.3	+6.3	2155.3	+8.3
		8.63	2095.0	2102.4	+7.4	2094.7	-0.3	2098.9	+3.9	2103.0	+8.0	2105.6	+10.6
39.00	1.88	0.0	2145.0	2141.5	-3.5	2136.1	-7.9	2141.5	-3.5	2141.9	-3.1	2142.4	-2.6
		8.63	2077.0	2084.6	+7.6	2079.2	+2.2	2082.3	+5.3	2085.2	+7.2	2085.5	+8.5
39.38	0.88	0.0	2132.0	2128.8	-3.2	2126.5	-5.5	2128.8	-3.2	2128.5	-3.5	2129.3	-2.7
		8.63	2062.0	2065.8	+3.8	2063.2	+1.2	2064.5	+2.5	2066.2	+4.2	2066.4	+4.4
39.75	0.0	0.0	2122.0	2122.0	0.0	2121.7	-0.3	2122.0	0.0	2122.0	0.0	2122.0	0.0
		8.63	2052.0	2048.7	-3.3	2048.6	-3.4	2048.7	-3.3	2048.9	-3.1	2048.9	-3.1

APPENDIX (C)

<u>FORTRAN VARIABLE</u>	<u>DEFINITION</u>
N	Maximum value of X direction index n
I	Maximum value of Y direction index i
J	Maximum value of Z direction index j
XL	Length of channel in X direction
YL	Length of channel in Y direction
ZL	Length of channel in Z direction
XEND	Value of X at which to terminate integration
RHO	Density of the glass
CP	Specific heat of the glass
TKP	Glass equivalent thermal conductivity in Y direction
TKPP	Glass equivalent thermal conductivity in Z direction
SIGMA	Stefan-Boltzmann Constant
H	Convective heat-transfer coefficient
ES	Emissivity of ceramic radiating surface
EG	Emissivity of the glass
TSI	Temperature of radiating boundary @ $X = 0$
T000	Initial plane corner temperatures
TOOW	
TODO	
TODW	
TLDW	Corner temperatures @ $x = XL$
TLOW	
TA	Temperature of the ambient gas
TC	Temperature of radiating surface along channel centerline
VMAX	Max. glass velocity for parabolic distribution
TODWR	Radiating surface Tem. @ $x = 0, y = YL, z = ZL$
TLDWR	Radiating surface Tem. @ $x = XL, y = YL, z = ZL$
IRNT	Counter for steady-state program printout control
NTERM	Number of terms to used in defining series for velocity calculation
ITR	Counter to recalculate the velocity array
ITRA	Counter for number of iterations for velocity convergence
ITRB	Counter used for non-converging velocities at the nodes
NUP	Counter to update the velocity array
WA	Weight factor for linear combination
T(i,j)	2-Dimensional temperature array

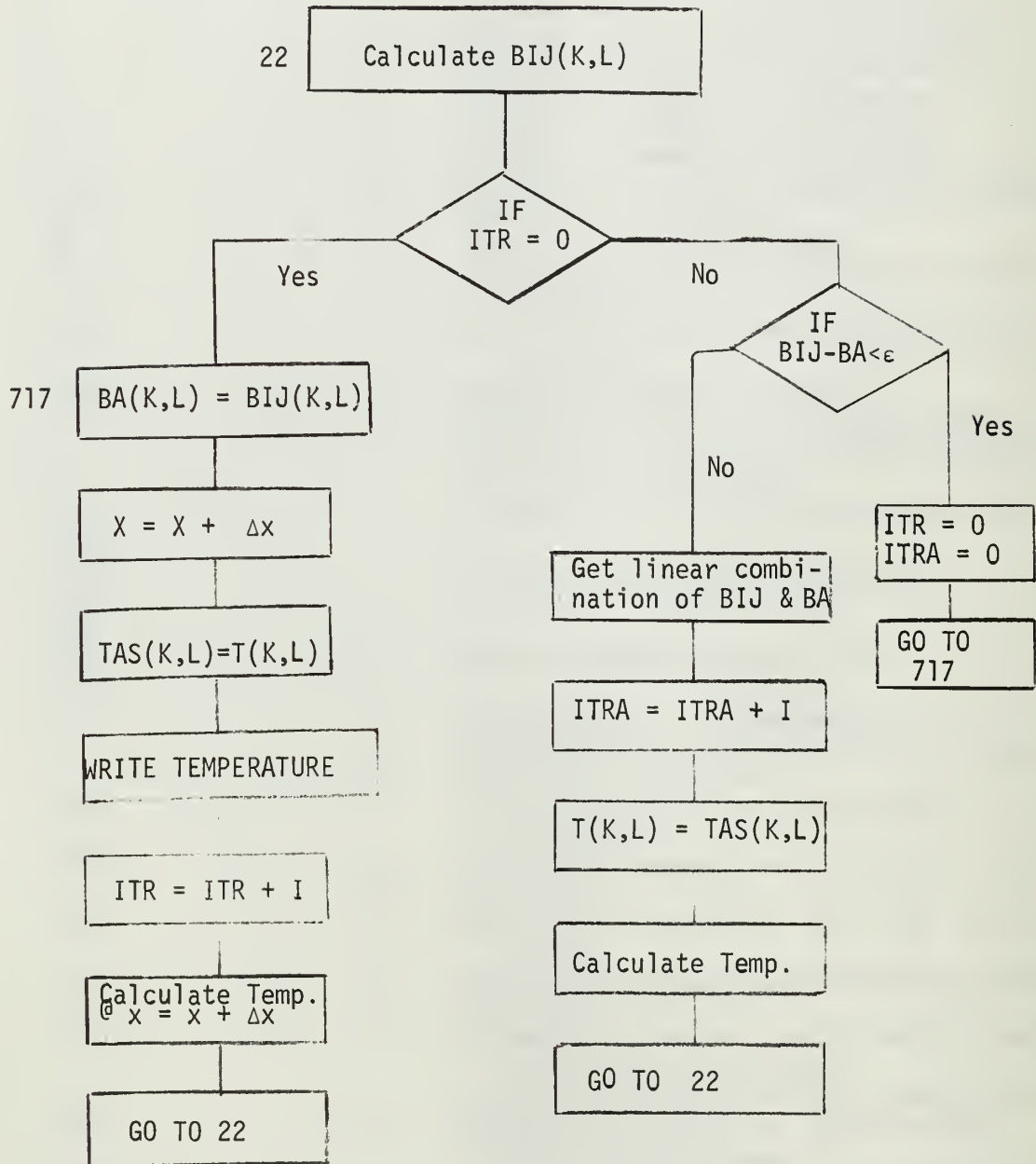
BIJ (i,j)	2-Dimensional array for glass velocity (V_x) in X direction at (i,j) points in y,z plane
BA (k,j)	2-Dimensional array for intermediate velocities
TAS (i,j)	2-Dimensional array to store tem. @ the former plane

APPENDIX (D)

FLOW GRAPH TO CALCULATE VELOCITIES

ITR = 0 (Set counters to zero)

ITRA = 0



C COMBINED STEADY-UNSTEADY STATE GLASS PROGRAMS.

```

1  DIMENSION T(45,100),BIJ(45,100),DEN1(45,100),DEN2(45,100),
1  TLAM(45,100),PREM(45,100),BA(45,100),TAS(45,100),H(30,75) ,
      JLOT(18),YP(50),TP(50),WD(18),DELS(8)
1  DIMENSION TU(30,15,15),S(30,15,15),ALFI(15),DENI(15),ALFJ(15)
1  DIMENSION A(30,15),B(30,15),DENJ(15),NOUT(12)
1  COMMON TU,N,I,J,IPRT,IYP,IZP
1  FORMAT (12I5)
2  FORMAT (4E15.6)
3  FORMAT (1H1,50X5HINPUT///,40X3HN=I6,4H I=I6,4H J=J6)
4  FORMAT (///,7X2HXL,13X2HZL,12X4HXEND,12X3HRHO,13X2HCP,
12X3HTKP,11X4HTKPP/8E15.5)
5  FORMAT (///,4X5HSIGMA,14X1HH,13X2HES,13X2HEG,12X3HTS1/5E15.5)
6  FORMAT (///,5X4HTODW,12X4HTODW,12X4HTODW,12X4HTODW,12X4HTL00,
12X4HTL0W,12X4HTLDW/8E16.5)
7  FORMAT (///,7X2HTA,14X2HTC,12X4HVMAX,11X5HTODWR,11X5HTLDWR/8E16.5)
9  FORMAT (///,7X7HJLOT(K)/18I5)
12  FORMAT (1H0,20X5HIYP=I2,5X5HIYP=I3,5X7HIPRT=I3)
13  FORMAT (///,6X4HDELX,12X4HDELY,12X4HDELZ,14X2HCL,14X2HC2/5E16.5)
14  FORMAT (1H1,5HTAPE READ HAS REACHED END POINT - START CALCULATION)
181  FORMAT (1H1,50X11HTEMP AT X=FF7.5)
182  FORMAT (1H0,50X11HTEMP AT X=FF7.5)
19  FORMAT (18F7.1)
191  FORMAT (17F7.1)
700  FORMAT(2E15.8)

```

C READ ARRAY AND SWITCHING(PATH) DATA

```

      READ(5,1) N,I,J,NTAPE,NBOTH,NTAPEA,NTIMEA
      READ(5,1) NPATHA,NPATHB,NTIME,IPRT,IYP,IZP,IPRNT

```

C THIS SECTION FOR TRANSIENT RUNS ONLY USING PRERECORDED RESULTS

```

201  GO TO(204,201),NTAPEA
      N=N/IPRT
      I=I/IYP
      J=J/IZP
      DO 202 M=1,N
      DO 203 L=1,J
      READ(15,19,END=1081) (TU(M,K,L),K=1,I)
      CONTINUE
      CONTINUE
      CALL DYNAL
      WRITE(5,14)
1081  CALL DYNAL

```


C INPUT-OUTPUT SECTION

```

204 READ (5,2) XL,YL,ZL,XEND,RHO,CP,TKP,TKPP
    READ (5,2) SIGMA,H,ES,EG,TS1
    READ (5,2) T000,T00W,T00D,T00D,T00D,TLOW,TLDW
    READ (5,2) TA,TC,VMAX,TODWR,TLDWR
    READ (5,1) (JLOT(K),K=1,18)
    READ(5,1) NTERM
    READ(5,700) PI,FRICA
    WRITE (6,3) N,I,J
    WRITE (6,4) XL,YL,ZL,XEND,RHO,CP,TKP,TKPP
    WRITE (6,5) SIGMA,H,ES,EG,TS1
    WRITE (6,6) T000,T00W,T00D,T00D,T00D,TLOW,TLDW
    WRITE (6,7) TA,TC,VMAX,TODWR,TLDWR
    WRITE (6,9) (JLOT(K),K=1,18)
    WRITE(6,12) IYP,IZP,IPRNT,IPRT

```

C INITIALIZATION AND CALCULATION OF VARIOUS SYSTEM CONSTANTS AND PARAMS

```

IRNT=IPRNT
ICNT=IPRT
IM1=I-1
JMI=J-1
DELX=XL/DELX
DELY=I
DELY=YL/DELY
DELY=J
DELY=ZL/DELY
CV1=2.0*DELY/YL*VMAX
CV2=DELY*DELY/ZL/ZL
CV3=DELY*DELY/ZL/ZL
C1=TKPP*0.5*DELY/DELY/RHO/CP
C2=TKPP*0.5*DELY/DELY/DELY/RHO/CP
WRITE (6,13) DELX,DELY,DELY,C1,C2
C12=2.0*C1
C22=2.0*C2
FRICB=(1.0-FRICA*FRICA)/(2.0*(1.0-FRICA))
FRIC=1.0/(1.0/FRICB+(1.0/ES-1.0)+(1.0/EG-1.0))
FH1=-C1*DELY*4.0*SIGMA*FRIC/TKP
FH3=-C1*DELY*H*TA/TKP
TH1=-C1*(1.0-H*DELY/TKP)
A1A=DELY*TC/XL
A2A=C1*C1
TS1=TS1+0.5*A1A

```

C CALCULATE BOUNDARY CONDITION CONSTANTS AND DO SOME INITIALIZATION

```

DELXH=0.5*DELX
WBI=(TLOW-T00W)/XL
WTI=(TLDW-T0DW)/XL
YCLI=(TLCO-T000)/XL
YORI=(TLOW-T00W)/XL
WTIR=(TLDWR-T0DWR)/XL
X=-DELX
M=1
KOUNT=1

```

C INITIALIZE T

```

NA=0
ITR=0
ITRA=0
ITRB=0
YN=1
Z=0.0
L=1
20 TTOP=T0D0+Z/ZL*(T0DW-T0D0)
TBOT=T000+Z/ZL*(T00W-T000)
TINC=(TTOP-TBOT)/YN
T(1,L)=TBOT+TINC
DO 21 K=2,I
21 T(K,L)=T(K-1,L)+TINC
L=L+1
Z=Z+DELZ
IF (L-J) 20,20,22

```

CALCULATE VELOCITY DISTRIBUTION DEPENDING ON TEMPERATURE DISTRIBUTION

```

22 SUMT=0.0
NUP=0
NLIM=INTERM*2-1
DO 703 K=1,I
DO 704 L=1,J
TLAM(K,L)=(135700.0)/(10.0**((9.072-0.00282*T(K,L)))
PREM(K,L)=TLAM(K,L)*0.129
CONTINUE
CONTINUE
AY=YL
DO 33 K=1,I
AY=AY-DELY
AZ=0.0
704
703

```

```

DO 32 L=1,J
SUMC=0.0
DO 702 N=1,NLIM,2
CUBE=N*N*N
NSIGN=(-1)**((N-1)/2)
ARG=(N*PI)/(2.0*YL)
T1=COSH(ARG*AZ)
T2=COSH(ARG*ZL)
T3=COS(ARG*AY)
T4=1.0-T1/T2
TERM=NSIGN*T4*T3/CUBE
SUMC=SUMC+TERM
CONTINUE
BIJ(K,L)=PREM(K,L)*SUMC
AZ=AZ+DELZ
CONTINUE
IF(ITR.EQ.NA) GOTO 717
ITRB=0
DO 730 K=1,I
DO 731 L=1,J
DELV=BA(K,L)-BIJ(K,L)
DELV=ABS(DELV)
FORMAT(8E16.5)
IF(DELV-0.05)731,731,791
ITRB=ITRB+1
CONTINUE
WRITE(6,1)ITRB
IF(ITRB.GT.NA)GO TO 714
WRITE(6,747)((BIJ(K,L),L=1,J),K=1,I)
ITR=0
ITRA=0
GO TO 717
WA=0.25
ITRA=ITRA+1
WRITE(6,1)ITRA
DO 715 K=1,I
DO 716 L=1,J
T(K,L)=TAS(K,L)
BIJ(K,L)=WA*BA(K,L)+(1.0-WA)*BIJ(K,L)
CONTINUE
DO 718 K=1,I
DO 719 L=1,J
BA(K,L)=BIJ(K,L)
CONTINUE

```

702

32

33

749

747

791

731

730

1000

714

716

715

717

719

718

```

C CALCULATE DEN2
DO 38 K=1, I
DO 37 L=1, J
IF (L-1) 34, 34, 35
34 DEN2(K, L)=1.0/(BIJ(K, L)+C22)
   ALF2=C22*DEN2(K, L)
   GO TO 37
35 DEN2(K, L)=1.0/(BIJ(K, L)+C22-C2*ALF2)
   IF (L-J) 36, 37, 37
36 ALF2=C2*DEN2(K, L)
37 CONTINUE
38 CONTINUE

C CALCULATE DEN1
DO 44 L=1, J
DO 43 K=1, IM1
IF (K-1) 39, 39, 40
39 DEN1(K, L)=1.0/(BIJ(K, L)+C12)
   ALF1=C1*DEN1(K, L)
   GO TO 43
40 DEN1(K, L)=1.0/(BIJ(K, L)+C12-C1*ALF1)
   ALF1=C1*DEN1(K, L)
43 CONTINUE
44 CONTINUE
   IF (ITRA.GT.NA) GO TO 25

C START LOOP
50 X=X+DELX
DO 712 K=1, I
DO 713 L=1, J
713 TAS(K, L)=T(K, L)
712 CONTINUE
GO TO(995, 998), NPATHA
995 IRNT=IRNT+1
   IF (IRNT-IPRNT) 56, 65, 65

C WRITE T
65 IRNT=C
998 IF (X.EQ.0.0) GO TO 999
998 GO TO(996, 997, 999), NPATHA
997 IF (X.LE.3.12) GO TO 56
   GO TO 999
996 IF (X.GE.3.12) NPATHA=2

```

```

999 IF(KOUNT-1) 994,994,993
994 WRITE(6,181) X
    KOUNT=2
    GO TO 992
993 WRITE(6,182) X
    KOUNT=1
992 YOLH=T000+X*YOLI
    YORH=T00W+X*YORI
    YOINC=(YORH-YOLH)/ZL*DELZ
    WBO=T00W+X*WBI
    WTO=T00W+X*WTI
    ZWINC=(WTO-WBO)/YL*DELY
    TEMPW=WBO-ZWINC
    IP1=I+1
    DO 69 K=1,IP1
    DO 67 L=1,18
    J1=JLOT(L)
    IF (J1) 68,68,66
    IF (K-1) 46,46,47
    66 D1=J1-1
    46 WD(L)=YOLH+D1*YOINC
    GO TO 67
    47 WD(L)=T(K-1,J1)
    67 CONTINUE
    L=18
    68 L=L-1
    TEMPW=TEMPW+ZWINC
    WRITE (6,191)(WD(LP),LP=1,L),TEMPW
    CONTINUE
    69 GO TO(25,661),NTIME
    56 ICONT=ICNT+1
    661 IF(ICNT-IPRT) 25,23,251
    23 GO TO(242,244),NTAPE
    244 DO 243 L=1,J,IZP
    243 WRITE(15,19) (T(K,L),K=IYP,I,IYP)
    242 CONTINUE
    242 GO TO(251,245),NBOTH
    245 LL=1
    DO 24 L=1,J,IZP
    KK=1
    DO 241 K=IYP,I,IYP
    TU(M,KK,LL)=T(K,L)
    KK=KK+1
    241 CONTINUE
    LL=LL+1
    24 CONTINUE
    M=M+1
    251 ICNT=0

```

```

C CHECK X VARIABLE VS. ITS END VALUE
25 IF (X-XEND) 70,105,105
C CALCULATE F*
70 DO 76 K=1,I
DO 75 L=1,J
LM1=L-1
IF (LM1) 71,71,72
71 TM1=T(K,2)
TNO=T(K,1)
TPI=TM1
GO TO 75
72 T(K,LM1)=C2*(TM1+TPI)+(BIJ(K,LM1)-C22)*TNO
IF (L-J) 74,73,73
73 T(K,L)=C2*TNO+(BIJ(K,L)-C22)*TPI
GO TO 75
74 TM1=TNO
TNO=TPI
TPI=T(K,L+1)
75 CONTINUE
76 TSI=TS1-A1A
TH2=(TS1-WTIR*(X+DELXH)-TODWR)*DELZ/ZL
FH2=TS1+460.0
PAR1=FH2
DO 41 L=1,J
DEN1(I,L)=1.0/(BIJ(I,L)+C12-A2A*DEN1(IM1,L)+TH1-FH1*PAR1**3)
PAR1=PAR1-TH2
41 CONTINUE
PAR1=FH2
PAR2=TS1
DO 77 L=1,J
T(I,L)=T(I,L)-FH3-FH1*PAR2*PAR1**3
PAR1=PAR1-TH2
PAR2=PAR2-TH2
77 CONTINUE
WBO=TODW+X*WBI
WTO=TODW+X*WTI
ZWINC=(WTO-WBO)/YL
DZINC=DELY*ZWINC*C2
D=WBO*C2
DO 78 K=1,I
D=D+DZINC
T(K,J)=T(K,J)+D
78 YOLH=TODW+(X+DELXH)*YOLI

```



```

YORH=TOOW+(X+DELXH)*YORI
YOINC=(YORH-YOLH)/ZL
DYINC=DELZ*YOINC*C1
D=YOLH*C1-DYINC
DO 79 L=1, J
D=D+DYINC
79 T(1,L)=T(1,L)+D

```

C CALCULATE BETA*

```

DO 84 L=1, J
DO 83 K=1, I
IF (K-1) 80,80,81
80 T(K,L)=T(K,L)*DEN1(K,L)
GO TO 82
81 T(K,L)=(T(K,L)+C1*BETO)*DEN1(K,L)
82 BETO=T(K,L)
83 CONTINUE
84 CONTINUE

```

C CALCULATE T*

```

DO 86 L=1, J
JML=J-L+1
DO 85 K=1, IM1
IMK=I-K
T(IMK,JML)=T(IMK,JML)+C1*T(IMK+1,JML)*DEN1(IMK,JML)
85 CONTINUE
86 CONTINUE

```

C CALCULATE F

```

87 PAR1=FH2
PAR2=TS1
DO 93 L=1, J
DO 92 K=1, I
KM1=K-1
IF (KM1) 88,88,89
88 TM1=0.0
TNO=T(1,L)
TP1=T(2,L)
GO TO 92
89 T(KM1,L)=C1*(TM1+TP1)+(BIJ(KM1,L)-C12)*TNO
IF (K-1) 91,90,90
90 PAR13=FH1*PAR1**3
T(K,L)=C1*TNO+(BIJ(K,L)-C12-TH1+PAR13)*TP1-FH3-PAR13*PAR2
PAR1=PAR1-TH2
PAR2=PAR2-TH2

```

```

91 GO TO 92
   TM1=TNO
   TNO=TP1
   TP1=T(K+1,L)
92 CONTINUE
93 D=YOLH*C1-DYINC
   DO 94 L=1,J
   D=D+DYINC
94 T(1,L)=T(1,L)+D
   WBN=TOOW+(X+DELX)*WBI
   WTN=TOOW+(X+DELX)*WTI
   ZWINC=(WTN-WBN)/YL
   DZINC=DELY*ZWINC*C2
   D=WBN*C2
   DO 95 K=1,I
   D=D+DZINC
95 T(K,J)=T(K,J)+D

C CALCULATE BETA
   DQ 100 K=1,I
   DO 99 L=1,J
   IF (L-1) 96,96,97
96 T(K,L)=T(K,L)*DEN2(K,L)
   GO TO 98
97 T(K,L)=(T(K,L)+C2*BETO)*DEN2(K,L)
98 BETO=T(K,L)
99 CONTINUE
100 CONTINUE

C CALCULATE T
   DO 104 K=1,I
   IMK=I-K+1
   DO 103 L=1,JM1
   JML=J-L
101 IF (JML-1) 101,101,102
   T(IMK,JML)=T(IMK,JML)+C22*T(IMK,2)*DEN2(IMK,JML)
102 GO TO 103
103 T(IMK,JML)=T(IMK,JML)+C2*T(IMK,JML+1)*DEN2(IMK,JML)
104 CONTINUE
   IF (ITRB.GT.NA) GO TO 22
   IF (NUP.EQ.50) GO TO 207
   NUP=NUP+1
   GOTO 50
207 ITR=ITR+1

```

GO TO 22

C STEADY-STATE PROGRAM DONE.EITHER STOP OR GO ON TO TRANSIENT PROGRAM.

```

105 GO TO (1052,1051),NTAPE
1051 END FILE 15
1052 GO TO (106,107),NTIMEA
107 CALL DYNAMO
106 STOP
END

```

C UNSTEADY STATE SECTION OF PROGRAM STARTS HERE.

```

SUBROUTINE DYNAMO
DIMENSION T(45,100),BIJ(45,100),DEN1(45,100),DEN2(45,100),
1 JLOT(18),YP(50),TP(50),WD(18)
DIMENSION TU(30,15,15),S(30,15,15),ALFI(15),DENI(15),ALFJ(15)
DIMENSION A(30,15),B(30,15),DENJ(15),NOUT(12)
DIMENSION TAU(4),CHANGE(4),TAUSB(3),CHGSB(3),DLYSB(3),TSBSS(3)
DIMENSION TIME(50),TPLT1(50),TPLT2(50),TPLT3(50),TPLT4(50),TPLT5(
150),TPLT6(50),TPLT7(50),TPLT8(50),TPLT9(50),TPLT10(50),TPLT11(50),
2 TPLT12(50)
COMMON TU,N,I,J,IPRT,IYP,IZP
1 FORMAT (12I5)
2 FORMAT (4E15.6)
4 FORMAT (F10.5,12F10.1)
5 FORMAT (///,4X5HSIGMA,14X1HH,13X2HES,13X2HEG/4E15.5)
6 FORMAT (///,5X4HTODW,12X4HTOD0,12X4HTODW/4E16.5)
7 FORMAT (///,7X2HTA,12X4HVMAX/2E16.5)
8 FORMAT (///,7X2HXL,14X2HYL,14X2HZL,13X4HTEND,13X3HRRHO,14X2HCP,
113X3HTKF,12X4HTKPP/8E16.5)
9 FORMAT (///,F19.3,F23.1,F11.1,F15.3)
10 FORMAT (1H1,50X5HINPUT//,40X3HN=16,4H I=16,4H J=16,5H NT=16)
11 FORMAT (1H0,7HPRINT=F7.3)
12 FORMAT (1H1,12X43HPOSITIONS OF TEMPERATURE READINGS IN INCHES//,4X4
1HTIME,5X7HX=39.75,3X7HX=39.38,3X7HX=39.00,3X7HX=38.25,3X7HX=37.88,
23X7HX=37.50,3X7HX=39.75,3X7HX=39.38,3X7HX=39.00,3X7HX=38.25,3X7HX=
337.88,3X7HX=37.50//,5X2HIN,6X5HY=0.0,5X6HY=1.88,4X6HY=3
4.88,4X6HY=4.88,4X6HY=5.88//,4X5HOURS,4X5HZ=0.0,5X5HZ=0.0,5X5HZ=0.0
588,4X6HZ=0.0,5X5HZ=0.0,5X6HZ=8.63,4X6HZ=8.63,4X6HZ=8.63,4X
6,5X5HZ=0.0,5X5HZ=0.0,5X6HZ=8.63,4X6HZ=8.63,4X6HZ=8.63,4X
76HZ=8.63,4X6HZ=8.63,4X6HZ=8.63,4X6HZ=8.63,4X6HZ=8.63,4X
13 FORMAT (//,6X4HDELX,12X4HDELY,14X2HCL,14X2HC2/5E16.5)

```

```

14 FORMAT (///,25X29HRADIATING BOUNDARY CONDITIONS//,35X14HTIME CONSTA
15 INTS//,10X7HTAU(1)=F8.5,7HTAU(2)=F8.5,7HTAU(3)=F8.5,7HTAU(4)=F8.5)
16 FORMAT (///,25X30HSTEADY-STATE VALUES AT TIME =0//,10X4HTS1=F7.1,
17 13HTC=F7.1,6HTODWR=F7.1,6HTLDWR=F7.1)
18 FORMAT (///,25X43HCHANGES IN STEADY-STATE VALUES AT MAX. TIME//,10X
19 11OHCHANGE(1)=F6.1,1OHCHANGE(2)=F6.1,1OHCHANGE(3)=F6.1,1OHCHANGE(4)
20 =F6.1)
21 FORMAT (1H1,25X36HSIDE-WALL-BOTTOM BOUNDARY CONDITIONS//,5X14HTIME
22 1CONSTANTS,5X18HSTEADY-STATE VALUE,5X6HCHANGE,5X10HDELAY(HRS))
23 FORMAT (1H1,10X11HTEMP AT X =F7.5,8H TIME =F7.5,7H TS1 =F7.1,
24 17H TS2 =F7.1,6H TC =F7.1,9H TODWR =F7.1,9H TLDWR =F7.1,///)
25 FORMAT (1H0,50X11HTEMP AT X =F7.5,8H TIME =F7.5,///)
26 FORMAT (1H1,50X11HTEMP AT X =F7.5,8H TIME =F7.5,///)

```

C CALCULATE ARRAY SIZE VARIABLES

```

N=N/IPRT
I=I/IYP
J=J/IYP

```

C ENTRY POINT FOR TRANSIENT RUNS ONLY USING PRERECORDED RESULTS

```

ENTRY POINT DYN1
NT
READ(5,1) (NOUT(L),L=1,12)
READ(5,1) XL,YL,ZL,TEND,RHO,CP,TKP,TKPP
READ(5,2) SIGMA,H,ES,EG
READ(5,2) T000,T00W,T00D,TODW
READ(5,2) TA,VMAX,PRINT
READ(5,2) (TAU(K),K=1,4)
READ(5,2) TSISS,TCSS,DWRSS,TLDWRS
READ(5,2) (CHANGE(K),K=1,4)
READ(5,2) (TAUSB(K),K=1,3)
READ(5,2) (TSBSS(K),K=1,3)
READ(5,2) (CHGSB(K),K=1,3)
READ(5,2) (DLYSB(K),K=1,3)
WRITE(6,10) N,I,J,NT
WRITE(6,8) XL,YL,ZL,TEND,RHO,CP,TKP,TKPP
WRITE(6,5) SIGMA,H,ES,EG
WRITE(6,6) T000,T00W,T00D,TODW
WRITE(6,7) TA,VMAX
WRITE(6,11) PRINT
WRITE(6,14) (TAU(K),K=1,4)
WRITE(6,15) TSISS,TCSS,DWRSS,TLDWRS
WRITE(6,16) (CHANGE(K),K=1,4)
DO 3 K=1,3

```

```

      WRITE(6,9)  TAUSB(K),TSBSS(K),CHGSB(K),DLYSB(K)
3  CONTINUE
C  INITIALIZATION AND CALCULATION OF VARIOUS SYSTEM CONSTANTS AND PARAMS

```

```

      KKK=1
      CNT=0.0
      IM1=I-1
      JM1=J-1
      IP1=I+1
      JP1=J+1
      DELT=NT
      DELT=TEND/DELT
      DELX=N
      DELX=XL/DELX
      DELY=I
      DELY=YL/DELY
      DELZ=J
      DELZ=ZL/DELZ
      CV1=DELY/YL*VMAX*DELT/DELX
      CV2=DELY*DELY/YL/YL*VMAX*0.5*DELT/DELX
      CV3=DELZ*DELZ/ZL/ZL
      C1=TKP*0.5*DELT/DELY/DELY/RHO/CP
      C2=TKPP*0.5*DELT/DELZ/DELZ/RHO/CP
      WRITE (6,13) DELX,DELY,DELZ,C1,C2
      C12=2.0*C1
      C22=2.0*C2
      C14=2.0*C12
      C24=2.0*C22
      A1=1.0-C14-C24
      FRIC=1.0/(1.0/ES+1.0/EG-1.0)
      C1A=4.0*SIGMA*FRIC*DELY/TKP
      C2A=DELY*H*TA/TKP
      C1B=C1A
      C2B=1.0-DELY*H/TKP

```

```

C  CALCULATE BIJ

```

```

      DO 533 K=1,I
      D=K
      VT1=CV1*D-CV2*D*D
      DO532 L=1,J
      D=L-1
      BIJ(K,L)=VT1*(1.0-CV3*D*D)
532 CONTINUE
533 CONTINUE

```

```

C  CALCULATE DENI AND DENJ

```



```

DENI(1)=-1.0/(1.0+C12)
ALFI(1)=C1/(1.0+C12)
DO523 K=2, IM1
DENI(K)=1.0/(C1*ALFI(K-1)-1.0-C12)
ALFI(K)=-C1*DENI(K)
CONTINUE
ALFI(1)=C1*ALFI(IM1)
DENJ(1)=-1.0/(1.0+C22)
ALFJ(1)=C22/(1.0+C22)
DO524 L=2, JM1
DENJ(L)=1.0/(C2*ALFJ(L-1)-1.0-C22)
ALFJ(L)=-C2*DENJ(L)
CONTINUE
524 DENJ(J)=1.0/(C2*ALFJ(JM1)-1.0-C22)

```

C CALCULATE VARIOUS SYSTEM CONSTANTS

```

XOTI=(TODW-T00W)/YL
XOBI=(TOD0-T000)/YL
ZWBI=(TODW-T00W)/YL
YOB1=(T00W-T000)/ZL
Q11=2.0/ZL
Q12=T00W-T000
Q13=XOTI-XOBI
Q14=2.0*T000
Q15=2.0*XOBI
Q21=1.0/XL
Q24=T000
Q25=YOBI
Q31=1.0/XL
Q34=T00W
Q35=ZWBI

```

C WRITE OUT INITIAL CONDITION DATA

```

X=0.0
Y=0.0
Z=0.0
U=0.0
WRITE (6,20) X,U
KOUNT=2
DO529 K=1, IP1
XOT=T00W+Y*XOTI
XOB=T000+Y*XOBI
Y=Y+DELY
WD(1)=XOB

```



```

WDI=(XOT-XOB)/ZL*DELZ
D0528 L=2,J
WC(L)=WD(L-1)+WDI
528 CONTINUE
529 WRITE(6,19) (WD(L),L=1,J),XOT
D0534 M=1,N
X=X+DELX
IF(KOUNT-1) 600,600,601
600 WRITE(6,20) X,U
KOUNT=2
GO TO 602
601 WRITE(6,183) X,U
KOUNT=1
602 YOLH=T000+X*(TSBSS(1)-T000)/XL
YORH=T00W+X*(TSBSS(2)-T00W)/XL
WDI=(YORH-YOLH)/ZL*DELZ
WD(1)=YOLH
ZWINC=TODW+X*(TSBSS(3)-TODW)/XL
ZWINC=(ZWINC-YORH)/YL*DELY
D0530 L=2,J
WD(L)=WD(L-1)+WDI
530 CONTINUE
WRITE(6,19) (WD(L),L=1,J),YORH
D0531 K=1,I
YORH=YORH+ZWINC
WRITE(6,19)(TU(M,K,L),L=1,J),YORH
531 CONTINUE
534 CONTINUE
GO TO 539

C START THE GRAND LOOP
525 U=U+DELT

C CALCULATE TIME DEPENDENT B.C. TERMS
TS1=TS1SS+CHANGE(1)*(1.0-EXP(-U/TAU(1)))
TS2=(TS1SS-TCSS)+CHANGE(2)*(1.0-EXP(-U/TAU(2)))
TC=TS1-TS2
TODWR=DWRSS+CHANGE(3)*(1.0-EXP(-U/TAU(3)))
TLDWR=TLDWRS+CHANGE(4)*(1.0-EXP(-U/TAU(4)))
CIT=TC/XL
WTIR=(TLDWR-TODWR)/XL
TL00=TSBSS(1)+CHGSB(1)*(1.0-EXP(-(U-DLYSB(1))/TAUSB(1)))
IF(U.LE.DLYSB(1)) TL00=TSBSS(1)
FLOW=TSBSS(2)+CHGSB(2)*(1.0-EXP(-(U-DLYSB(2))/TAUSB(2)))
IF(U.LE.DLYSB(2)) FLOW=TSBSS(2)

```

```

TLDW=TSBSS(3)+CHGSB(3)*(1.0-EXP(-(U-DLYSB(3))/TAUSB(3)))
IF(U.LE.DLYSB(3)) TLDW=TSBSS(3)
WBI=(TLOW-T00W)/XL
WTI=(TLDW-T0DW)/XL
YOLI=(TLOO-T000)/XL
YORI=(TLOW-T00W)/XL
ZWTI=(TLDW-TLOW)/YL
YOTI=(TLOW-TLOO)/ZL
Q22=TLOO-T000
Q23=YOTI-YOBI
Q32=TLOW-T00W
Q33=ZWTI-ZWBI

```

C PREPARE RADIATING B.C. TERMS

```

X=DELX
D0536 M=1,N
Z=0.0
D0535 L=1,J
TS=TS1-C1I*X+Z/ZL*(TODWR-TS1+X*(WTIR+C1I))
TS3=(TS+460.0)**3
A(M,L)=C1A*TS3*TS+C2A
B(M,L)=C2B-C1B*TS3
Z=Z+DELZ
535 CONTINUE
X=X+DELX
536 CONTINUE

```

C CALCULATE T*(THIS IS THE RECURSION SECTION OF THE PROGRAM)

```

Y=DELY
D0560 K=1,I
Z=0.0
D0559 L=1,J
X=DELX
BIJC=BIJ(K,L)
A1MB=A1-BIJC
DIV=1.0+BIJC
D0558 M=1,N
D=TU(M,K,L)*A1MB
IF (M-1) 545,545,546
D=D+BIJC*(Q11*Z*(Q12+Q13*Y)+Q14+Q15*Y)
GO T0547
545 D=D+BIJC*(S(M-1,K,L)+TU(M-1,K,L))
546 D=D+BIJC*(S(M-1,K,L)+TU(M-1,K,L))
547 IF (K-1) 548,548,549
548 D=D+C12*(TU(M,2,L)+Q21*X*(Q22+Q23*Z)+Q24+Q25*Z)
GO T0552
549 IF (K-1) 551,550,550

```

```

550 D=D+C12*(TU(M,IM1,L)+A(M,L)+TU(M,I,L)*B(M,L))
551 GO T0552
552 D=D+C12*(TU(M,K-1,L)+TU(M,K+1,L))
553 IF (L-1) 553,553,554
554 D=D+C24*TU(M,K,2)
555 GO T0557
556 IF (L-J) 556,555,555
557 D=D+C22*(TU(M,K,JM1)+Q31*X*(Q32+Q33*Y)+Q34+Q35*Y)
558 GO T0557
559 D=D+C22*(TU(M,K,L-1)+TU(M,K,L+1))
560 S(M,K,L)=D/DIV
561 X=X+DELX
562 CONTINUE
563 Z=Z+DELZ
564 CONTINUE
565 Y=Y+DELY
566 CONTINUE
567 CONTINUE

C CALCULATE F**
D0567 L=1,J
D0568 M=1,N
D0569 K=1,I
IF (K-1) 561,561,562
561 S(M,1,L)=C1*TU(M,2,L)-C12*TU(M,1,L)-S(M,1,L)
562 GO T0565
563 IF (K-1) 564,563,563
564 S(M,I,L)=C1*TU(M,IM1,L)+(C1*B(M,L)-C12)*TU(M,I,L)-S(M,I,L)
565 GO T0565
566 S(M,K,L)=C1*(TU(M,K-1,L)+TU(M,K+1,L))-C12*TU(M,K,L)-S(M,K,L)
567 CONTINUE
568 CONTINUE

C CALCULATE BETA**
D0575 L=1,J
D0576 M=1,N
BETO=0.0
D0577 K=1,I
IF (K-1) 571,570,570
570 S(M,I,L)=(S(M,I,L)-C1*BETO)/(ALFI(I)+C1*B(M,L)-1.0-C12)
571 GO T0573
572 S(M,K,L)=(S(M,K,L)-C1*BETO)*DENI(K)
573 BETO=S(M,K,L)
574 CONTINUE
575 CONTINUE

```

```

C   CALCULATE T**
    DO578 L=1,J
    DO577 M=1,N
    DO576 K=1,IM1
    IMK=I-K
    S(M,IMK,L)=S(M,IMK,L)+ALFI(IMK)*S(M,IMK+1,L)
576 CONTINUE
577 CONTINUE
578 CONTINUE

C   CALCULATE F
    DO585 K=1,I
    DO584 M=1,N
    DO583 L=1,J
    IF (L-1) 579,579,580
    S(M,K,L)=C22*(TU(M,K,2)-TU(M,K,1))-S(M,K,1)
579 GO TO583
580 IF (L-J) 582,581,581
581 S(M,K,J)=C2*TU(M,K,JM1)-C22*TU(M,K,J)-S(M,K,J)
582 S(M,K,L)=C2*(TU(M,K,L-1)+TU(M,K,L+1))-C22*TU(M,K,L)-S(M,K,L)
583 CONTINUE
584 CONTINUE
585 CONTINUE

C   CALCULATE BETA
    DO591 K=1,I
    DO590 M=1,N
    BETO=0.0
    DO589 L=1,J
    TU(M,K,L)=(S(M,K,L)-C2*BETO)*DENJ(L)
    BETO=TU(M,K,L)
589 CONTINUE
590 CONTINUE
591 CONTINUE

C   CALCULATE T
    DO594 K=1,I
    DO593 M=1,N
    DO592 L=1,JM1
    JML=J-L
    TU(M,K,JML)=TU(M,K,JML)+ALFJ(JML)*TU(M,K,JML+1)
592 CONTINUE

```

```

593 CONTINUE
594 CONTINUE

C WRITE TEMPERATURE
  CNT=CNT+1.0
  IF (CNT-PRINT) 537,527,527

527 DO543 MOUT=1,12
  M=NOUT(MOUT)
  IF (M) 539,539,544

544 X=M
  X=X*DELX
  IF(KOUNT-1) 603,603,604
  WRITE(6,18) X,U,TS1,TS2,TC,TODWR,TLDWR
  KOUNT=2
  GO TO 605

604 WRITE(6,183) X,U
  KOUNT=1

605 YOLH=T000+X*YOLI
  YORH=T00W+X*YORI
  WDI=(YORH-YOLH)/ZL*DELZ
  WD(1)=YOLH
  ZWINC=TODW+X*WTI
  ZWINC=(ZWINC-YORH)/YL*DELY
  DO541 L=2,J
  WD(L)=WD(L-1)+WDI

541 CONTINUE
  WRITE (6,19) (WD(L),L=1,J),YORH
  DO542 K=1,I
  YORH=YORH+ZWINC
  WRITE (6,19) (TU(M,K,L),L=1,J),YORH

542 CONTINUE
543 CONTINUE
539 TIME(KKK)=U
  TPLT1(KKK)=WD(1)
  TPLT2(KKK)=0.1536*TU(25,3,1)+0.0464*TU(24,3,1)+0.6144*TU(25,2,1)+0
  1.1856*TU(24,2,1)
  TPLT3(KKK)=0.3696*TU(25,5,1)+0.3304*TU(24,5,1)+0.1584*TU(25,4,1)+0
  1.1416*TU(24,4,1)
  TPLT4(KKK)=0.0399*TU(25,10,1)+0.6601*TU(24,10,1)+0.0171*TU(25,9,1)
  1+0.2829*TU(24,9,1)
  TPLT5(KKK)=0.1648*TU(24,13,1)+0.0352*TU(23,13,1)+0.6592*TU(24,12,1)
  1)+0.1408*TU(23,12,1)
  TPLT6(KKK)=0.4095*TU(24,15,1)+0.2905*TU(23,15,1)+0.1755*TU(24,14,1)
  1)+0.1245*TU(23,14,1)
  TPLT7(KKK)=WD(11)
  TPLT8(KKK)=0.1536*TU(25,3,11)+0.0464*TU(24,3,11)+0.6144*TU(25,2,11)
  1)+0.1856*TU(24,2,11)

```


LIST OF REFERENCES

1. International Business Machine Corp., System Development Div., Report 02-472-1, Glass Container Process; Forehearth Simulation by J. Duffin and K. Johnson, 19 July 1965.
2. Kellet, B. S., Steady Flow of Heat Transfer Through Hot Glass, Journal of the Optical Society of America, V. 42, p. 339-343, 21 Nov. 1951.
3. Chapman, A. J., Heat Transfer, p. 334-335, The McMillan Company, 1960.
4. Douglas, Jim, Jr. and D. W. Peaceman, Numerical Solution of Two-Dimensional Heat-Flow Problems, A.I.Ch.E. Jour. V.I., p. 505-507, Dec. 1955.
5. Douglas, Jim, Jr., Advances in Computers, Vol. 2, p. 37-38, Academic Press, 1961.
6. Cooper, A. R., Jr., Effect of Aspect Ratio and Viscosity Gradients on Flow Through Open Channels, Jour. Am. Ceramic Soc., Vol. 43, No. 2, p. 97-104, 19 August 1959.
7. Timoshenko, Stephen and J. N. Goodier, Theory of Elasticity, 2nd ed., p. 275, McGraw-Hill, 1951.
8. Glass Container Industry Research Corporation, Preliminary Study of the Mathematical Model for the Control of Forehearth by T. H. Finger, (Chart 529), 1966.

INITIAL DISTRIBUTION LIST

	No. Copies
1. Defense Documentation Center Cameron Station Alexandria, Virginia 22314	20
2. Library, Code 0212 Naval Postgraduate School Monterey, California 93940	2
3. Professor J. H. Duffin Department of Material Science & Chemistry Naval Postgraduate School Monterey, California 93940	1
4. LTJG Sina Pekcelen Cevizlik Niyazi Bey Sok No. 24 Bakirkoy-Istanbul Turkey	5
5. Department of Material Science & Chemistry Naval Postgraduate School Monterey, California 93940	3
6. Commander, Naval Ordnance Systems Com. Hqs. Department of the Navy, Washington D.C. 20360	1

UNCLASSIFIED

Security Classification

DOCUMENT CONTROL DATA - R & D

(Security classification of title, body of abstract and indexing annotation must be entered when the overall report is classified)

1. ORIGINATING ACTIVITY (Corporate author)
Naval Postgraduate School
Monterey, California 93940

2a. REPORT SECURITY CLASSIFICATION

UNCLASSIFIED

2b. GROUP

3. REPORT TITLE

Verification of Model of Molten Glass Flow in a Forehearth

4. DESCRIPTIVE NOTES (Type of report and inclusive dates)

Master's Thesis, December 1969

5. AUTHOR(S) (First name, middle initial, last name)

Sina Pekcelen

6. REPORT DATE

December 1969

7a. TOTAL NO. OF PAGES

60

7b. NO. OF REFS

8

8a. CONTRACT OR GRANT NO.

b. PROJECT NO.

c.

d.

9a. ORIGINATOR'S REPORT NUMBER(S)

9b. OTHER REPORT NO(S) (Any other numbers that may be assigned this report)

10. DISTRIBUTION STATEMENT

This document has been approved for public release and sale; its distribution is unlimited.

11. SUPPLEMENTARY NOTES

12. SPONSORING MILITARY ACTIVITY

Naval Postgraduate School
Monterey, California 93940

13. ABSTRACT

In this work, variations on velocity profiles in a flowing mass of molten glass in a forehearth are investigated. Formerly used parabolic velocity profiles are replaced with analytical solution of open channel flow equation, based on the available data on mass flow of molten glass through the channel in unit time.

Concerning the viscosity effects; temperature dependence of viscosity is built in the model. However, it is assumed that the depth of the channel does not affect the viscosity gradients.

To solve the system of non-linear differential equations i.e., heat equation and flow equation; the analytical solution of the latter at the nodes is used for the numeric solution of the former iteratively, until the convergence is obtained. Predicted temperatures are compared to the available data from an actual operating forehearth, and against the results predicted by the previous model using simplifying assumptions to prove its validity.

14.

KEY WORDS

LINK A

LINK B

LINK 6

[illegible]

WT

ROLE

WT

ROLE

W 9

Forehearth Simulation
Molten Glass Flow
Math. Model - Numerical Analysis
Coupled Partial Differential Eqs. (Non-Linear)

thesP32738

Verification of model of molten glass fl



3 2768 001 97931 3

DUDLEY KNOX LIBRARY